

**QP Code : 5579**

Time 03 hours.

Max Marks: 80

Instructions to candidate

1. Q 1 is compulsory
2. Attempt any **THREE** from remaining
3. Figures to the right indicate full marks
4. Assume suitable data if necessary

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|------|---|----|
| 1    | a) Explain concept of power spectral density  | 5  |
|      | b) state and prove Central Limit Theorem  | 5  |
|      | c) Explain properties of cross correlation function                                       | 5  |
|      | d) state and prove Bayes' theorem   | 5  |
| 2 a) | Box 1 contains 5 white balls and 6 black balls. Box 2 contains 6 white & 4 black balls    | 10 |
|      | A box is selected at random and then a ball is chosen at random from the selected         |    |
|      | Box (i) What is the probability that the ball chosen will be a white ball                 |    |
|      | (ii) Given that the ball chosen is white what is the probability that came from box 1     |    |
|      | b) Give the properties of CDF, pdf, and PMF.  | 10 |
| 3 a) | Explain concept of conditional probability and properties of conditional probability      | 10 |
|      | b) Explain what do you mean by?   | 03 |
|      | (i) Deterministic system  |    |
|      | (ii) stochastic system  |    |
|      | (iii) Memoryless system   |    |
|      | c) Prove that if input to memoryless system is strict sense stationary (SSS) process then | 07 |
|      | output is also strict sense stationary  |    |
| 4 a) | Explain Random process, define ensemble mean, Auto correlation and Auto covariance of     |    |
|      | the process in terms of indexed random variables in usual mathematical forms              | 10 |
|      | b) Let $Z=X+Y$ Determine pdf of Z $f_z(Z)$  | 10 |
| 5 a) | state and prove Chapman Kolmogorov equation   | 10 |
|      | b) Explain Chebyshev's Inequality with suitable example.                                  | 10 |

TURN OVER

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6) a) The joint probability density function of two random variables is given by

$$F_{xy}(x, Y) = 15 e^{-3x-3y} ; x \geq 0, y \geq 0$$

- i) Find the probability that  $x < 2$  and  $Y > 0.2$
- ii) Find the marginal densities of X and Y
- iii) Are X and Y independent?
- iv) Find  $E(x/y)$  and  $E(y/x)$

10

b) Write short Notes on following special distributions

- i) Poisson distributions
- ii) Rayleigh distributions
- iii) Gaussian distributions

10

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